

Equivalent Representations of the F-FCSR Keystream Generator

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SASC 2008 - The State of the Art of Stream Ciphers
February 13–14, 2008
Lausanne, Switzerland

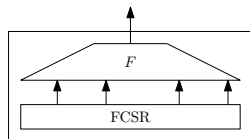
The F-FCSR Stream Cipher Family (Arnault et al.)

The F-FCSR ciphers consist of

- a regularly clocked (Galois) Feedback with Carry Shift Register (FCSR) with n register cells

- a linear filter function

$$F : \{0, 1\}^n \rightarrow \{0, 1\}^k$$

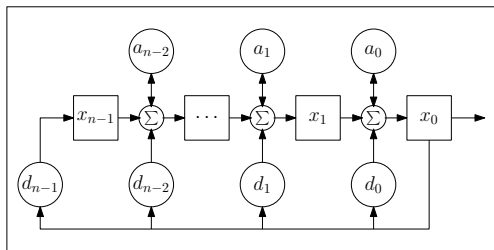


Proposed instances:

	k	n	keylength [bits]	IV length [bits]
F-FCSR-H	8	160	80	[32, 80]
F-FCSR-16	16	256	128	[0, 128]

We can assume the initial FCSR-state produced by key/IV-setup to be periodic.

FCSR in Galois Architecture



In each clock cycle,
 $x_i := \sigma_i \bmod 2$
 $a_i := \sigma_i \operatorname{div} 2$
 with
 $\sigma_i := x_{i+1} + a_i d_i + x_0 d_i$

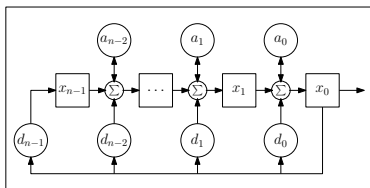
Identify the state (x, a) with $p := x + 2a$ and assume that the connection integer $q := 1 - 2d$ is prime.

At time $t \geq 0$ we have

- current state $p^t = 2^{-t} p^0 \bmod q$
- current output bit $z^t = p^t \bmod 2$.

for an initial state $p^0 = p$.

Sequences produced by individual Register Cells



Lemma (Arnault et al.):

$(x_i^t)_{t \geq 0}$ is given by the output sequence of a Galois FCSR with connection integer q and initial state $p_i = F_i(x, a) \cdot q + M_i(q) \cdot p$.

Observation

For periodic states (x, a) , p_i can be simplified to $p_i = p^{s_i} \pmod q$ with $s_i = -\log_2(M_i(q))$.

Implications:

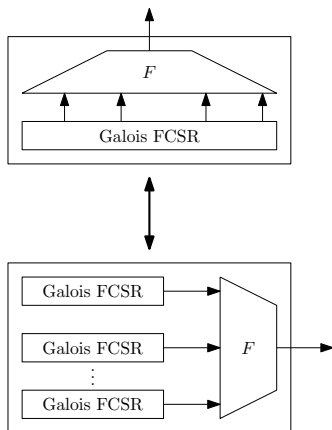
- $(x_i^t)_{t \geq 0}$ is a shifted version of $(z_i^t)_{t \geq 0}$.
- The phase shift s_i is independent of the initial state (x, a) .

Equivalent F-FCSR Representation (1)

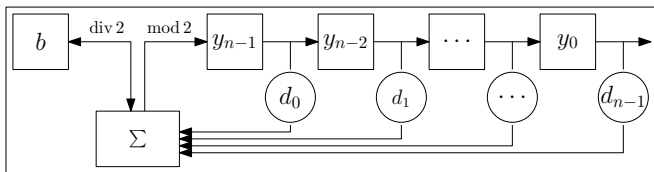
F-FCSR can be written as a combination generator with

- the original filter function F
- n Galois FCSRs with related initial states $p_i = p^{s_i}$

However: Experiments for F-FCSR-H show that the shifts s_i are distributed over a large part of the period.



FCSR in Fibonacci Architecture



Identify the state (y, b) with

$$p := b2^n - \sum_{k=0}^{n-1} \sum_{j=0}^k d_{j-1} y_{k-j} 2^k$$

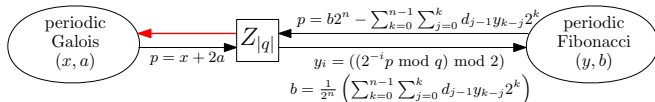
and assume that the connection integer $q = 1 - 2d$ is prime. As in the Galois architecture, we have for $t \geq 0$

- current state $p^t = 2^{-t} p^0 \pmod{q}$
- current output bit $z^t = p^t \pmod{2}$.

Mappings between Galois FCSRs and Fibonacci FCSRs

Problem: For a given periodic Galois state (x, a) find a periodic Fibonacci state (y, b) (and vice versa) such that the corresponding registers produce the same sequence.

Mappings:

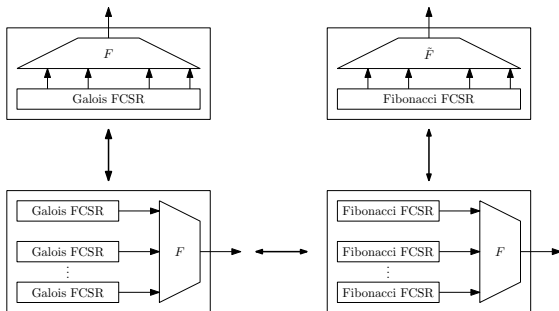


Observation

For each $0 \leq p < |q|$ and a prime connection integer q , the only periodic Galois initial state (x', a') with $x' + 2a' = p$ is given by

- $x'_i = M_i \cdot p \bmod q$ for $0 \leq i < n$
- $a' = \frac{p - x'_0}{2}$

Equivalent Representation (2)



More equivalent representations:

- Fibonacci FCSRs in the combination generator
- Fibonacci FCSR and modified (non-linear) filter function \tilde{F} in the filter generator

Remark: Fibonacci FCSR with linear filter is insecure.

Summary and Conclusion

We can transform the F-FCSR ciphers into equivalent

- combination or filter generators
- using Galois or Fibonacci FCSRs.

Currently, we see no efficient way to exploit these representations for cryptanalytic attacks,

... but maybe somebody else does?

The End.

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